

Liverpool John Moores University

Title: COMPLEX DYNAMICS
Status: Definitive
Code: **6008MATHS** (117483)
Version Start Date: 01-08-2016

Owning School/Faculty: Applied Mathematics
Teaching School/Faculty: Applied Mathematics

| Team | Leader |
|-----------------|--------|
| Paul Strickland | Y |

Academic Level: FHEQ6 **Credit Value:** 24 **Total Delivered Hours:** 72
Total Learning Hours: 240 **Private Study:** 168

Delivery Options

Course typically offered: Standard Year Long

| Component | Contact Hours |
|-----------|---------------|
| Lecture | 24 |
| Practical | 48 |

Grading Basis: 40 %

Assessment Details

| Category | Short Description | Description | Weighting (%) | Exam Duration |
|----------|-------------------|--|---------------|---------------|
| Report | AS1 | Alternative representations of 3D rotations and interpolation. | 25 | |
| Report | AS2 | Advanced matrix algebra. | 25 | |
| Report | AS3 | Applications of Chaos and Fractals. | 50 | |

Aims

An ability to analyse a range of real-world applications of number systems beyond the reals.

Identification of areas where complex dynamics apply, and associated computation.

Development of 3- and higher dimensional intuition through appropriate tools.

Learning Outcomes

After completing the module the student should be able to:

- 1 Identify and analyse abstract and real systems which exhibit chaotic behaviour.
- 2 Construct fractals from simple patterns and replication rules.
- 3 Calculate the generalised dimension of a set.
- 4 Perform calculations relating to different representations of rigid body transformations.
- 5 Apply the algebra of square matrices.

Learning Outcomes of Assessments

The assessment item list is assessed via the learning outcomes listed:

| | | | |
|--------------------|---|---|---|
| 3D rotations | 4 | | |
| Matrix algebra | 5 | | |
| Chaos and Fractals | 1 | 2 | 3 |

Outline Syllabus

Rigid movements in 3D space
Euler Angle
Complex Numbers and Quaternions
Eigenvalues and Eigenvectors
The Cayley-Hamilton theorem.
Orthogonal matrices in higher dimensions
One-dimensional dynamical systems.
The Mandelbrot set and its associated Julia sets.
Fractals via replication rules.
Examples of approximate fractals in nature.
Fractals with a random element.
Applications in computer graphics.
Towards a definition of chaos

Learning Activities

Students will use appropriate mathematical software to develop their understanding of the subject area.

Notes

This module will enable the students to apply advanced mathematical techniques to 3D graphics and the analysis of dynamical systems.

